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Treatment of low strength sewage with high suspended organic matter content in an anaerobic sequencing batch reactor and modeling application

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Abbreviations: α: particulate organic matter fraction

ASBR: anaerobic sequencing batch reactor CSTR: continuous stirred tank reactor COD: chemical oxygen demand IA: intermediate alkalinity OLR: organic load rate PA: partial alkalinity pCOD: particulate COD sCOD: soluble COD TA: total alkalinity tCOD: total COD TSS: total suspended solids UASB: up-flow anaerobic sludge blanket VFA: volatile fatty acid VSS: volatile fatty acid

In this work, an anaerobic sequencing batch reactor (ASBR) was operated for 8 months to treat low strength sewage with high suspended organic matter content. Three phases of operation with increasing organic loading rates (OLR) were performed: 0.4 kg COD/m³ x d (phase I), 0.8 kg COD/m³ x d (phase II) and 1.2 kg COD/m³ x d (phase III). Adequate stability parameters (pH, total alkalinity) were obtained through all three

experimental phases. During phases I and II, the removal efficiencies of organic matter (expressed as total chemical oxygen demand (COD) and total suspended solids ranged between 50-60%. However, these values decreased to 15-25% in phase III. In addition, a non-complex model, including hydrolysis, acidogenesis and methanogenesis, was applied to predict the reactor behavior.

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Figure 1. Scheme of the experimental system implemented for the anaerobic treatment of low strength sewage with high suspended organic matter content.

Anaerobic digestion processes have been mainly applied to high strength wastes and wastewaters, such as winery effluents, brewery slurries or sludge from wastewater treatment plants. Low strength wastewaters, like sewage, have not been extensively treated in anaerobic systems, although some reactors are operating in tropical countries.

Anaerobic reactors are an attractive alternative for sewage treatment in small communities not only due to low investment and operational costs, but also due to the low amounts of sludge produced and the energy recovered (*i.e.* biogas production).

The anaerobic treatment of these effluent types using continuous reactors (continuous stirred tank reactor (CSTR), upflow anaerobic sludge bed (UASB), etc) presents two main disadvantages. First, the organic matter concentrations are in the same range or only slightly higher than the affinity constant values for anaerobic biomass (K_s), and therefore the microorganisms do not work at high specific growth rates according to the Monod equation. Second, if a high fraction of particulate or suspended organic matter is present, the overall reaction slows down even further since hydrolysis of the complex particulates must occur first, which can become the limiting step of the whole process.

Anaerobic sequencing batch reactors (ASBR), developed by Sung and Dague (1995), are anaerobic systems which work in five-stage cycles: feeding, reaction, settling, discharge and idle time. These reactors have several advantages compared to continuous systems. At the beginning of the reaction stage, the organic matter concentration is at its maximum level, which in turn maximizes the degradation rate since the substrate concentration is greater than the affinity constant. In addition, several feeding strategies can be applied allowing batch, fed-batch or a combination of both (Zaiat et al. 2001), and the reaction and settling steps occur in the same tank. ASBRs have been mainly applied for the treatment of high strength wastes (Ruiz et al. 2002; Massé et al. 2003; Mockaitis et al. 2006; Ndegwa et al. 2008), although some studies with low strength wastewaters have also been performed (Bodik et al. 2002). The main drawback would be that the batch operation is not feasible for continuously discharged effluents. However, this situation might be overcome by using ASBRs in parallel.

The benefits of the implementation of mathematical models in wastewater treatment systems have been described by



Figure 2. Simplified anaerobic digestion process used in the model.



Figure 3. ASBR performance treating low strength sewage with high suspended organic matter content. a) *t*COD: (\circ) influent and (\bullet) effluent; b) *s*COD: (\Box) influent and (\bullet) effluent; c) TSS: (Δ) influent and (\bullet) effluent; d) Alkalinity: (\Box) TA, (\bullet) partial alkalinity (PA) and (\diamond) IA; e) VFAs: (\bullet) Acetic acid, (Δ) Propionic acid and (\circ) Butyric acid of the effluent.

many authors (Dochain and Vanrolleghem, 2001; Batstone et al. 2002). Different models have been applied in ASBRs, which were mainly validated with readily biodegradable and high-strength substrates. Most of them required many kinetic parameters and large systems of differential equations, and were therefore difficult to use for control purposes (Bagley and Brodkorb, 1999; Massé and Droste, 2000). Bernard et al. (2001) developed a simplified model using only two populations, acidogenic and methanogenic, which considerably reduced the number of kinetic parameters. Moreover, a great number of studies have been performed to determine the kinetic parameters of the acidogenic and methanogenic populations using different substrates, such as lactose, glucose, oils, solid vegetable wastes and volatile fatty acids (VFAs) (Bernard et al. 2001; Batstone et al. 2002). The values obtained for the different parameters varied among the different studies, due to the different specific experimental conditions used in each case.

The aim of this study was to evaluate the performance of an ASBR for the treatment of very low strength synthetic wastewater with high suspended organic matter content. Additionally, a simplified model with reported kinetic parameters was evaluated to predict the system behavior.

MATERIALS AND METHODS

Experimental set-up

A double-jacked reactor with a 4.0 L effective volume was used. It was operated at 35°C, using a thermostatically regulated water bath, with 1 h-cycles consisting of 20 min of feeding, 30 min of settling, 45 min of discharge and 10 min of idle time. The reaction times varied according to the organic load rate (OLR) applied, *i.e.* 1335 min, 615 min and 375 min, respectively. The reactor was mixed during the reaction stage by mixed-liquor recirculation in order to improve the mass transfer between the biomass and



Figure 4. sCOD concentrations during the reaction stage of: (a) phase I; (b) phase II; (c) phase III; (d) VFA concentration variation: (**a**) Acetic acid (\circ) Propionic acid and (**b**) Butyric acid and (**c**) pH; (e) VFA-COD equivalent during the reaction stage of phase III.

substrate. Peristaltic pumps were used for feeding, effluent discharge and mixed liquor recirculation.

Due to the low strength of the synthetic wastewaters used in this study, unreliable results of biogas production were obtained (data not shown). This was also reported previously (Ruiz et al. 2001; Rodrigues et al. 2003) even using more concentrated wastewaters (5 g COD/L). In these studies, the biogas production was estimated either with an empirical model or from off-line measurements of COD, volatile fatty acids (VFA) or suspended solids.

The system operated for 8 months and three phases were performed with increasing OLR: $0.4 \text{ kg COD/m}^3 \text{ x d } (1 \text{ space of } 1 \text{ spac$

cycle/d), 0.8 kg $COD/m^3 x d$ (2 cycles/d) and 1.2 kg $COD/m^3 x d$ (3 cycles/d). Each OLR was maintained until the pseudo-steady state (constant removal efficiencies) was achieved. The automated operation of the system (pumps, valves and mixer) was programmed in Microwin STEP7 using a PLC Siemmens® S7200. Figure 1 shows a diagram of the implemented system.

Wastewater and inoculum

The reactor feed was prepared synthetically and its composition was as follows: potato solution 4.0 g/L, ovoalbumin 0.12 g/L, vegetable oil 0.025 g/L and urea 0.033 g/L. In addition, both macro (NH₄Cl 0.074 g/L and



Figure 5. Comparison between modeled data (-) and experimental data (-). Total (a) and soluble (b) COD and acetic acid (c) concentrations.

KH₂PO₄ 0.01 g/L) and micronutrients (FeCl₃·4H₂O 0.004 g/L, ZnCl₂ 1 x 10^{-4} g/L, MnCl₂·4H₂O 0.001 g/L, CoCl₂·6H₂O 0.004 g/L, CuCl₂·2H₂O 6·10⁻⁵ g/L, NiCl₂·6H₂O 1 x 10^{-4} g/L, H₃BO₃ 1 x 10^{-4} g/L, Na₂SeO₃·2H₂O 2 x 10^{-4} g/L and (NH₄)6MoO₂·4H₂O 1.8 x 10^{-4} g/L) were included in the formulation. To maintain alkalinity, 0.5 g/L NaHCO₃ was also added.

The reactor was seeded with sludge from a lab-scale UASB reactor treating synthetic ethanol wastewater, whose methanogenic activity was 0.62 g $COD_{CH4}/gVSS \ x \ d$. The final concentration of biomass in the reactor was 5 g VSS/L.

Analytical methods

The pH, total (*t*COD) and soluble (*s*COD) COD, total suspended solids (TSS) and volatile suspended solids (VSS) and total alkalinity (TA) and intermediate alkalinity (IA) were determined according to standard methods (APHA, 1995). Samples for *s*COD and VFAs were filtered through glass-fiber filters prior to testing (Whatman GF/C). VFAs were determined by gas chromatography. Methane production was measured by liquid displacement (NaOH solution). The methanogenic activity test was performed in 100 mL serum bottles with a 1.5 g VSS/L biomass concentration, using the method developed by Soto et al. (1993)

Mathematical model

The model evaluated included three phases (hydrolysis, acidogenesis and methanogenesis), was based on the model developed by Bernard et al. (2001) (Figure 2) and has already been used in previous studies for other substrates (Keshtkar et al. 2001).

To develop and implement the model, some assumptions were made: feeding, settling, discharge and idle times were not considered in the model, since the durations were assumed negligible compared to reaction time and the operational conditions did not facilitate the degradation of organic matter. The biomass concentration in the reactor at the beginning of each cycle is the same. At the end of each cycle, all non-degraded particulate matter settled to the bottom of the reactor and accumulated for the next cycle (*i.e.* S = 1).

A simple mass balance for a batch reactor is shown in equation 1.

$$\frac{d\xi}{dt} = k_i \cdot r_{\xi}$$
[Eq. 1]

 ξ : state variable

 k_i : stoichiometric factor

 r_{ζ} : reaction rate

Despite more complex models that have been suggested (Vavilin et al. 2008), hydrolysis was considered as a first order kinetic reaction (equation 2), as recommended by most studies (Batstone et al. 2002). For acidogenesis and methanogenesis, a Monod-like model (equation 3) and a

Haldane-like model including the inhibition by volatile fatty acids (equation 4) were considered, respectively.

$$r_0 = k_0 \cdot X_0 \cdot X_{1 \text{[Eq. 2]}}$$

 r_0 : rate of hydrolysis reaction (d⁻¹)

 k_0 : hydrolysis catalytic constant (d⁻¹)

 X_0 : suspended organic matter concentration (g/L)

 X_1 : acidogenic biomass concentration (g/L)

$$r_1 = \boldsymbol{\mu}_1 \cdot \boldsymbol{X}_1 = \left(\boldsymbol{\mu}_{1M} \cdot \frac{\boldsymbol{S}_1}{\boldsymbol{K}_{S1} + \boldsymbol{S}_1} \right) \cdot \boldsymbol{X}_1$$
[Eq. 3]

 r_1 : Rate of acidogenic reaction (g/L·d).

 μ_1 : Specific growth rate of acidogenic biomass (d⁻¹).

 μ_{1M} : Maximum specific growth rate of acidogenic biomass (d^{-1}) .

S₁: Soluble organic matter concentration (g/L).

 K_{S1} : Affinity constant of acidogenic biomass (g/L).

$$r_{2} = \mu_{2} \cdot X_{2} = \left(\mu_{2M} \cdot \frac{S_{2}}{K_{S2} + S_{2} + \frac{S_{2}^{2}}{K_{12}}} \right) \cdot X_{2}$$

[Eq. 4]

 r_2 : Rate of methanogenic reaction (g/L·d).

 μ_2 : Specific growth rate of methanogenic biomass (d⁻¹).

X₂: Methanogenic biomass concentration (g/L).

 μ_{2M} : Maximum specific growth rate of methanogenic biomass (d⁻¹).

K_{S2}: Affinity constant of methanogenic biomass (mmol/L).

 K_{12} : Inhibition constant of methanogenic biomass (mmol/L).

S₂: Acetic acid concentration (mmol/L).

The system of equations was solved with Matlab® Software (Matrix Laboratory). From the uploaded input variables (*t*COD, *s*COD, VFAs and alkalinity), the model calculated the outputs, *i.e.* the effluent characteristics. The initial conditions considered were: an initial biomass

concentration of 5 g VSS/L, the methanogenic population accounting for 25% of the total, a *t*COD of 0.5 g/L, with 0.35 g/L and 0.15 g/L particulate COD (*p*COD) and soluble COD (*s*COD), respectively; and the VFA concentrations were assumed to be negligible.

RESULTS AND DISCUSSION

ASBR operation

Figure 3 shows the reactor performance during the 240 days of operation. The *t*COD,*s*COD and TSS levels in the influent varied between 300-600 mg/L, 100-200 mg/L and 200-400 mg/L, respectively. TSS content in the effluent was not affected by the OLR applied (around 100 mg/L). However, the COD concentrations remained almost constant during the first two phases, around 150 mg *t*COD/L and 50 mg *s*COD/L, but increased to 300 and 200 mg/L, respectively, in the last phase. Organic matter removal efficiencies decreased from 50-60% (phases I and II) to 15-25% (phase III), which was probably due to the shorter phase III reaction time, which caused the reactor to work as a hydrolytic-acidogenic system. In contrast, the suspended solids removal efficiency increased slightly from 40-50% (phases I and II) to 60-70% (phase III).

The reactor pH remained constant during the experimental period with values around 7.19 ± 0.11 , 7.26 ± 0.18 and 7.17 ± 0.15 in phases I, II and III, respectively. As shown in Figure 3d, the alkalinity levels remained constant in phases I and II (around 600 mg/L of TA), indicating process stability. In phase III, even though the IA (related to VFA concentration) increased slightly, the total and partial alkalinity did not vary significantly, thus indicating that the process remained stable.

In phases I and II, VFA concentrations in the effluent were negligible (Figure 3e), which indicates that the reaction time allowed the methanogenesis to proceed. However, in phase III, only the hydrolysis and acidogenesis occurred because no methanogenic activity was detected. The specific methanogenic activity diminished from 0.69 ± 0.01 $gCOD_{CH4}/gVSS$ x d in phase I to 0.55 \pm 0.01 gCOD_{CH4}/gVSS x d in phase II, and disappeared completely in phase III. The main reason for the methanization blockage might be the shorter reaction time applied in phase III, because it is known that the methanogenic population grows slower than acidogenic bacteria. From Figure 4d, the acidogenic rate was noticeably greater than the methanogenic rate during the reaction time. During this latter phase, acetic acid was the main component of VFA, reaching concentrations of up to 200 mg/L, which at this level are not expected to inhibit methanization.

Bodik et al. (2002) studied the performance of an ASBR treating domestic wastewater, obtaining an organic matter removal efficiency of 88%. The reactor influent was raw domestic wastewater supplemented with glucose and



Figure 6. Variation (%) of soluble (a) and total (b) COD concentrations at the end of the reaction time with k_0 at the three OLRs studied. Results obtained during model validation were used as reference.

acetate, which comprised about 60% of the feeding COD, thus reaching a final total COD feed concentration of 650 mg/L. These treatment conditions were significantly more advantageous for anaerobic digestion. Alvarez et al. (2004) treated domestic wastewater (tCOD: 330 - 360 mg/L) in an UASB reactor reaching total COD removal efficiencies of 60%. Lew et al. (2004) reported COD removal efficiencies up to 75% in a two-phase system (UASB + anaerobic filter) operated at high OLR (around 5 kg COD/m³ x d); however, solids accumulation in both reactors occurred. Ratusznei et al. (2001) treated synthetic domestic wastewater in an anaerobic sequencing batch biofilm reactor (ASBBR) with low total suspended solids (TSS) concentration, achieving total COD removal efficiencies of 85%, but at a lower OLR (around 0.3 kg $COD/m^3 \cdot d$) than those applied in this study $(0.4-1.2 \text{ kg COD/m}^3 \text{ x d})$. Sarti et al. (2007) studied two different mixing systems in a pilot ASBR treating domestic wastewater, at a similar OLR range to the range applied in this study. The reactor with liquid recirculation showed a lower tCOD removal efficiency (40%) than that obtained in the present work, while the values obtained in the ASBR operated with mechanical mixing were similar (60%).

Figure 4 shows the variation of *s*COD concentration during the reaction stage of each phase of operation. In phase I (Figure 4a), *s*COD concentrations decreased during the first 3 hrs, indicating a quick degradation of the soluble organic matter present in the influent. Afterwards, the *s*COD increased due to the solubilization of the suspended organic matter during the hydrolysis step. Finally, the *s*COD decreased and provided the VFA degradation. Similar behavior was found in phase II (Figure 4b), although methanogenesis did not occur completely. During these two phases, the VFA concentrations were close to the analytical method detection limit (data not shown).

However, a different profile was obtained for phase III (Figure 4c), where *s*COD increased quickly within the first

hour due to hydrolysis and remained constant for the rest of the reaction stage. Figure 4d shows the VFA level variation during the reaction stage of this last phase. The acetic acid levels increased continuously up to approximately 200 mg/L, whereas propionic and butyric acid concentrations remained constant with low values (< 40 mg/L). Assuming negligible activity of the methanogenic population, the ASBR VFA productivity during this acidogenic-hydrolytic operation (phase III) can be determined. Two clear zones can be differentiated (Figure 4e). In the first zone (first 1 hr), the VFA productivity was almost 10 times higher than in the second zone, showing the fast acidification of the *s*COD present in the influent. In the second zone (last 7 hrs), the hydrolysis of suspended organic matter likely limited the acidification process.

Model evaluation

Table 1 shows the kinetic parameters used for the model evaluation, which were selected from several studies carried out at operational conditions similar to the present work. All yield coefficients were taken from Bernard et al. (2001).

Figure 5 shows the comparison between the experimental and modeled data. During the first 30 days (phase I), the model predicted lower values of tCOD than the data obtained experimentally (Figure 5a). This result can be explained by the fact that the second assumption made related to biomass concentration at the beginning of each cycle was not met, since the biomass settleability was very poor during the first days of operation and a continuous washout occurred. At the beginning of phase III, the model also predicted a tCOD lower than the experimental values, which is related to the instability of the system after the increase in the OLR; in contrast, more stable experimental values were closer to the modeled ones.

Kinetic parameters	Unit	Value	Substrate	Reference
μ _{1m}	d ⁻¹	1.20	-	Bernard et al. (2001)
µ _{2m}	d⁻¹	0.74	Glucose	Bernard et al. (2001)
K ₁₂	mg/L	300	Winery wastewater	Batstone et al. (2004)
K _{S1}	mg/L	500	Manure/oil	Angelidaki et al. (1999)
K _{S2}	mg/L	213.4	Acetate	Vavilin et al. (1996)
k ₀	d ⁻¹	0.99	Primary sludge	Ristow et al. (2006)

Table 1. Kinetic parameters.

A better correlation was obtained for the *s*COD (Figure 5b), although some deviations were also seen during phase II and at the beginning of phase III. This was probably due to the presence of other soluble compounds not defined in the model, such as ethanol or lactic acid.

Despite the low acetic acid concentrations measured, an appropriate correlation between the experimental and modeled results was obtained. The higher experimental values obtained during phase III compared to the modeled ones might be explained by the fact that the model considers that all the VFAs are in the form of acetic acid, while small concentrations of propionic and butyric acid were also found experimentally. These results suggest that the acetic acid oxidation rates were somewhat underestimated by the model, which would partially explain the lower acetate concentrations.

Deviations between the modeled data and experimental results obtained in ASBR reactors have been encountered by other authors as well. Batstone et al. (2004) used the ADM1 model to determine and validate kinetic parameters treating two synthetic wastewaters, based on ethanol and acetate, respectively. The pH and biogas production values obtained during some consecutive cycles were used for the parameters fit, and a good correlation between the modeled and the experimental data was obtained for the first cycles of operation. However, the results became worse after 6 weeks of operation, due to the assumption that the biomass concentration remains constant which is more critical for highly concentrated effluents. Similar profiles were achieved by Bagley and Brodkorb (1999), who, after 10 cycles of operation using glucose as substrate, observed substantial deviations between the modeled and the experimental data.

Sensitivity analysis

A wide range of hydrolysis catalytic constant (d^{-1}) (k₀)values have been reported, from 0.005 d⁻¹(Christ et al. 2000) to 0.76 d⁻¹(Shimizu et al. 1993) using lipids as substrate or 0.99 d⁻¹(Ristow et al. 2006) using primary sludge. The latter was used in this study. On the other hand, the fraction of particulate organic matter determined in this study was 0.7 (70%); however particulate organic matter may undergo variations due to seasonal factors or uncontrolled industrial effluent dumping.

Figure 6 and Figure 7 show the effect of the k_0 and particulate organic matter fraction (α), respectively, on the *s*COD (Figure 6a and Figure 7a) and *t*COD (Figure 6b and Figure 7b) concentration variation at the end of the reaction time. As a reference, the results obtained during model validation were used.

Lower k_0 values than those used during model validation had an important effect on the ASBR performance, mainly on the *t*COD concentrations. The significant decrease in the *s*COD level indicates the accumulation of *p*COD in the sludge blanket, and thus the reduction of the total activity of the anaerobic biomass. This effect was more noticeable at the highest OLR applied (OLR3). These results indicate that the underestimation of k_0 could impair the model prediction severely. In contrast, an overestimation of the k_0 values did not affect the model results.

In general, α slightly affected the process results (Figure 7). A small under or overestimation (up to 30%) resulted in very low *s*COD and *t*COD variations (up to 15%). Higher variation of α value gave rise to a maximum variation of *s*COD and *t*COD of 15 and 30%, respectively.



Figure 7. Variation (%) of the soluble (a) and total (b) COD concentrations at the end of the reaction time with α at the three OLRs studied. Results obtained during model validation were used as reference.

CONCLUDING REMARKS

The anaerobic treatment of low strength sewage with high suspended organic matter content, in an ASBR reactor was successful up to an OLR of around 1 kg $COD/m^3 x d$ resulting in total COD removal efficiencies of 50-60%. Higher OLR values (1.2 kg $COD/m^3 x d$) provoked the washout of the methanogenic biomass, thus causing the reactor to behave as a hydrolytic-acidogenic system.

A simplified model, considering two populations and three processes, was developed and implemented to predict ASBR performance. The resulting model predicted quite accurately the reactor behavior during the 8 month experimental period in terms of COD and acetic acid concentrations. Deviations were due to biomass washout, which was not considered in the model.

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